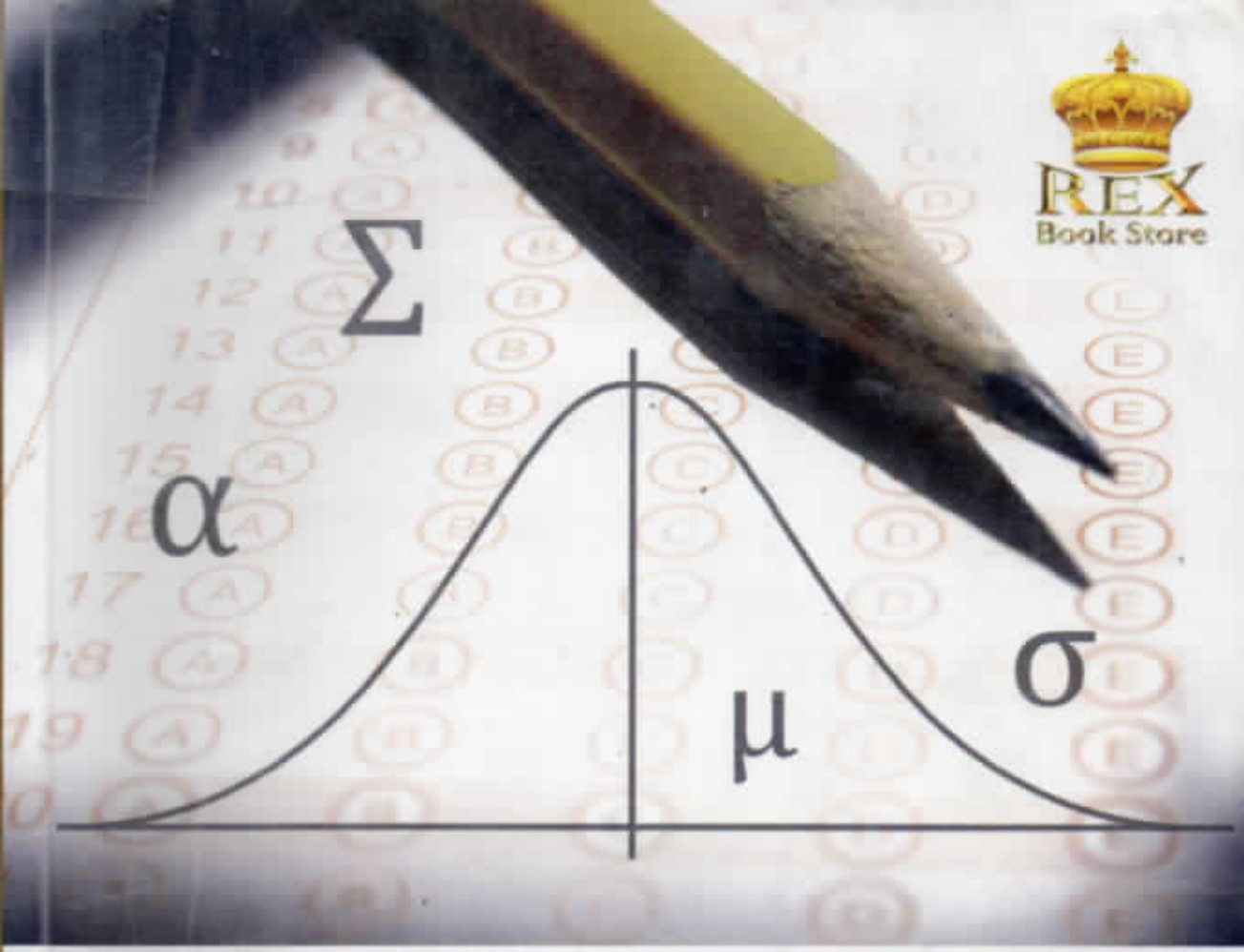

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STATISTICS AND PROBABILITY

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CORE

K TO 12

First Edition

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